



# Probabilistic Risk Awareness (PRA) Framework to Generate Early-Warning Signals of COVID-19

Bank of Canada COVID-19 Webinar

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**Nasim Rahaman** (Mila, Max-Planck-Institute for Intelligent Systems Tübingen)

**Andrew Williams** (Université de Montréal)

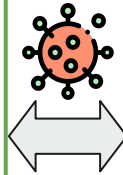
# COVID -19 has posed a novel social planning problem

Health policy experts:

Min COVID-19 transmission ( $R_t$ )

S.t

- Keep society functioning
- Minimize deaths



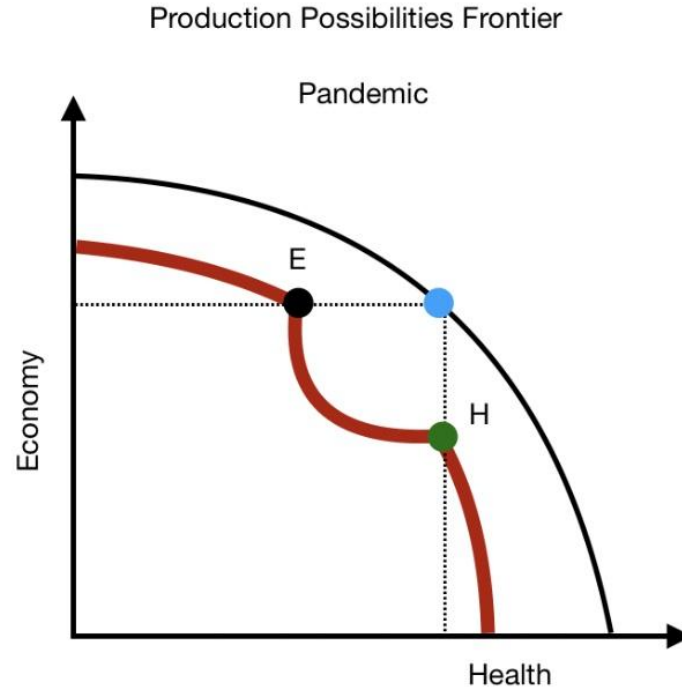
Economists:

Max Social Welfare

S.t

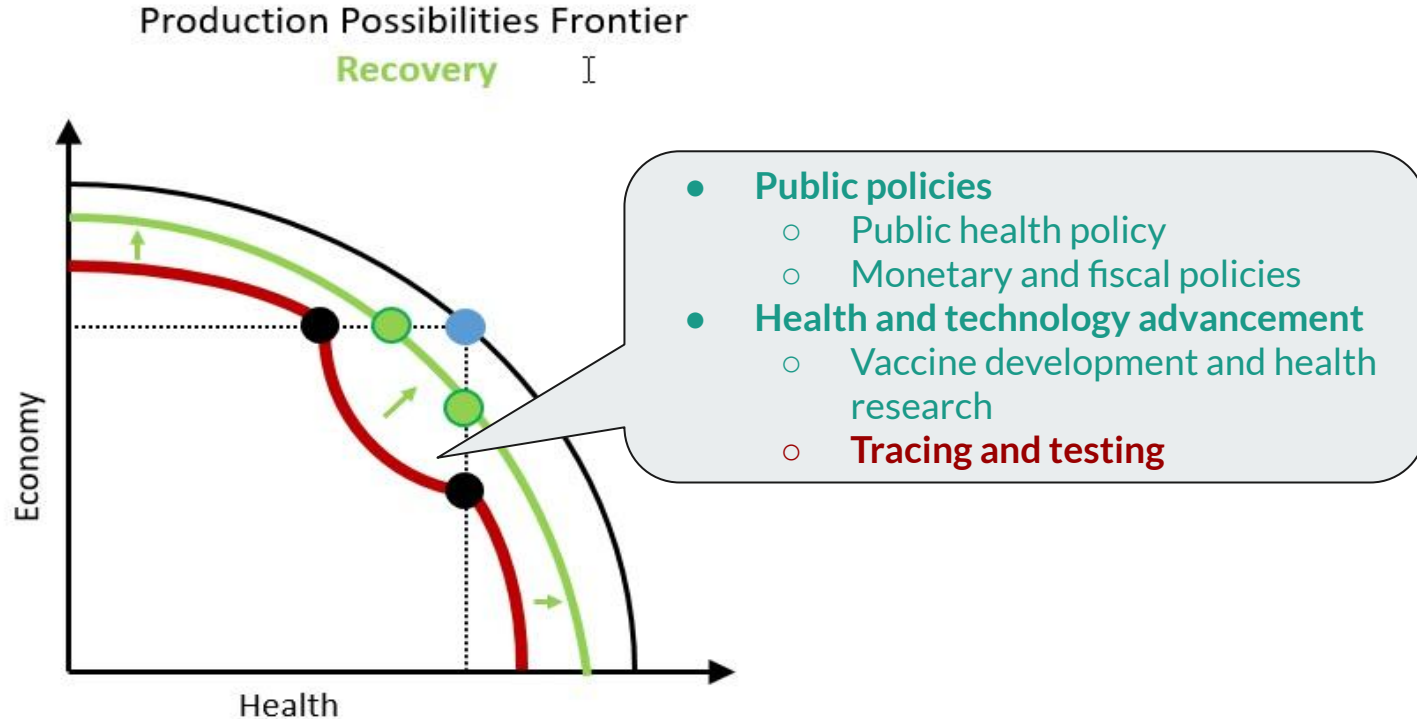
- Technological constraints
- Incentive constraints

# Inefficient economic and health outcome following COVID



Source: Gans( 2020), "Health Before Wealth: the Economic Logic", March 25, 2020  
<https://blog.usejournal.com/health-before-wealth-the-economic-logic-9c5414ae259c>

# How could we expand the frontier during the pandemic?



*Optimizing policy coordination calls for advanced technology*

# Roadmap of the talk



- Probabilistic Risk Assessment (PRA) Framework for Tracing
- A Machine / Deep Learning approach to PRA
- An Application of PRA to Economic and Health Assessment
- Conclusion and ongoing research

# COVI (Source code coming soon...)

## COVI White Paper - Version 1.0

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<https://arxiv.org/abs/2005.08502>

# ML/Epi/Econ Team



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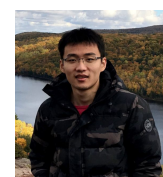
Joanna Merckx



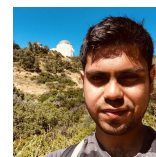
Nanoy Minoyan



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Meng Qu



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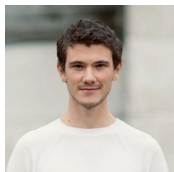


Christopher Pal

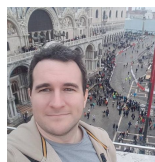
Pierre-Luc Carrier

Olexa Bilanuik

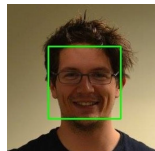
Marc-André Rousseau



Victor Schmidt



Pierre-Luc St  
Charles



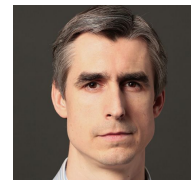
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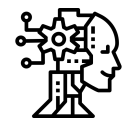


Joumana Ghosn

Gaetan Marceau Caron

# Built Upon An Agent-Based Epidemiological Model

Agents

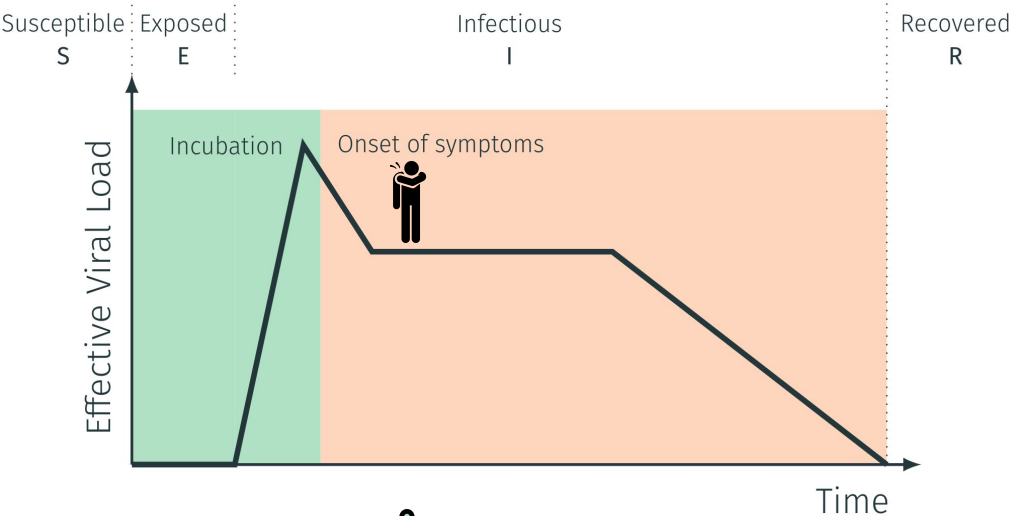


Contagiousness  
or  
Effective Viral Load

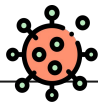


Susceptible  
Exposed  
Infectious  
Recovered

Incubation  
(Avg: 5 days)



Index Case



Secondary Case



# What we observe...

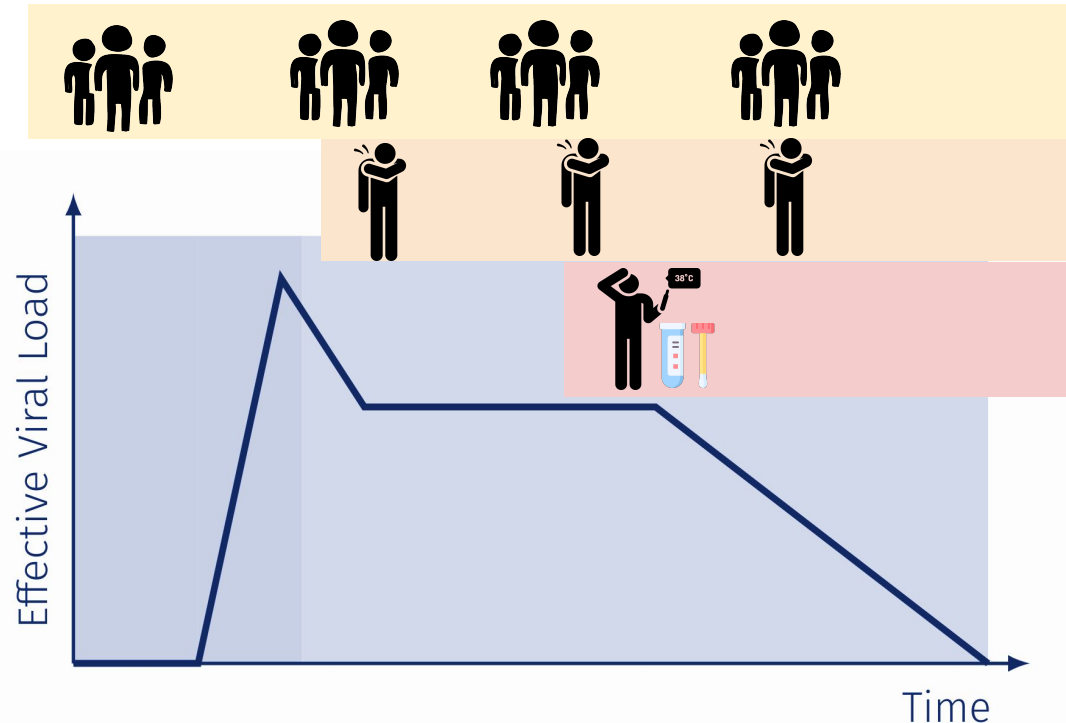
Contacts

Symptoms

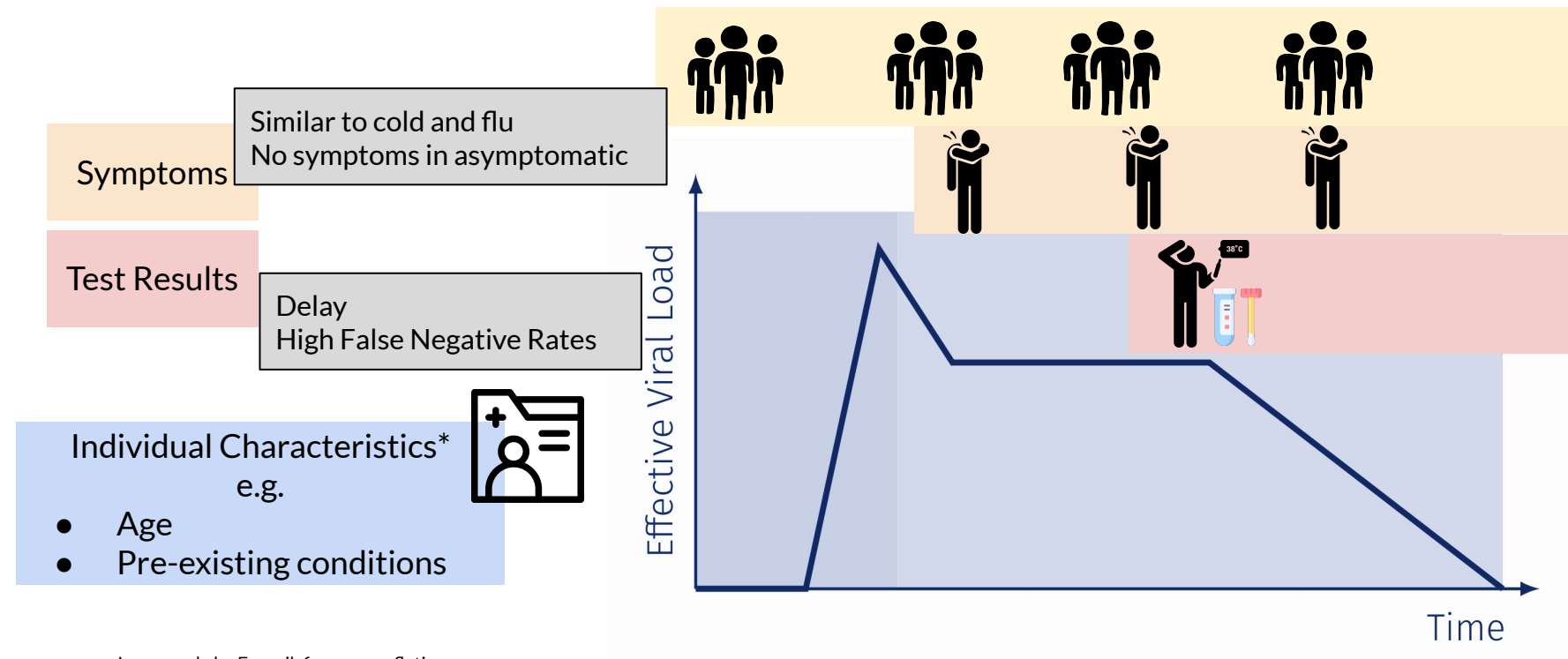
Test Results

Individual Characteristics\*  
e.g.

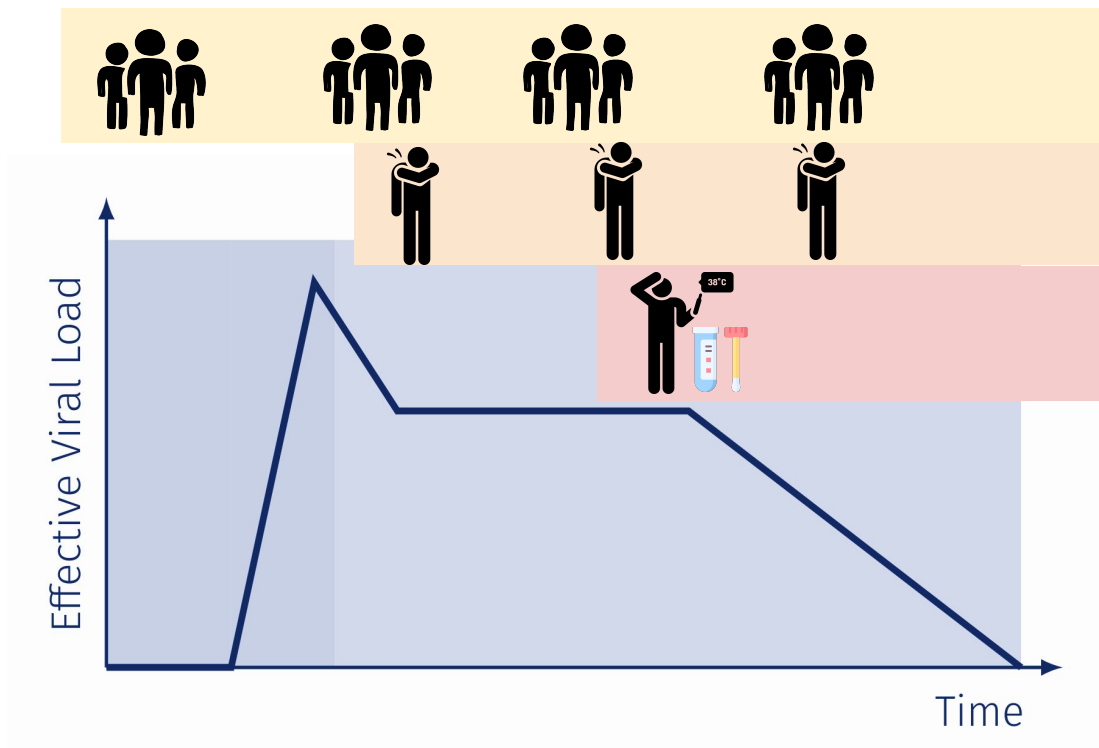
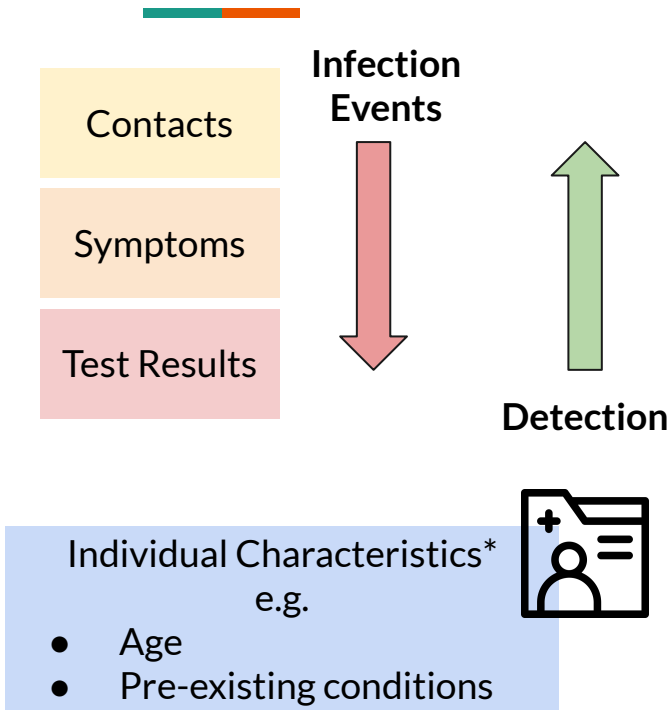
- Age
- Pre-existing conditions



# Noise in observations...






# Contact Tracing













# Landscape of tracing methods



















	 <b>Manual Tracing</b>	<b>Digital Binary Tracing (BDT)</b> 	<b>PRA (COVI)</b> 
<b>Potential Contacts</b>			
<b>Clues Used</b>			
<b>Recommendations</b>			


























# Manual Tracing is subject to memory challenges

	 <b>Manual Tracing</b>	<b>Digital Binary Tracing (BDT)</b> 	<b>PRA (COVI)</b> 
<b>Potential Contacts</b>	 		
<b>Clues Used</b>	  		
<b>Recommendations</b>	 		

# BDT provides precise contacts info, yet lacking some individual clues

	 Manual Tracing	Digital Binary Tracing (BDT) 	PRA (COVI) 
Potential Contacts	 	 	
Clues Used	  	 	
Recommendations	 	 	

# COVI encompasses BDT and profits from richer info from ABM

	 <b>Manual Tracing</b>	<b>Digital Binary Tracing (BDT)</b> 	<b>PRA (COVI)</b> 
Potential Contacts	 	 	 
Clues Used	  	 	   
Recommendations	 	 	  

# Probabilistic Risk Awareness (PRA): Framework



Predict **today's and past contagiousness** using all the clues



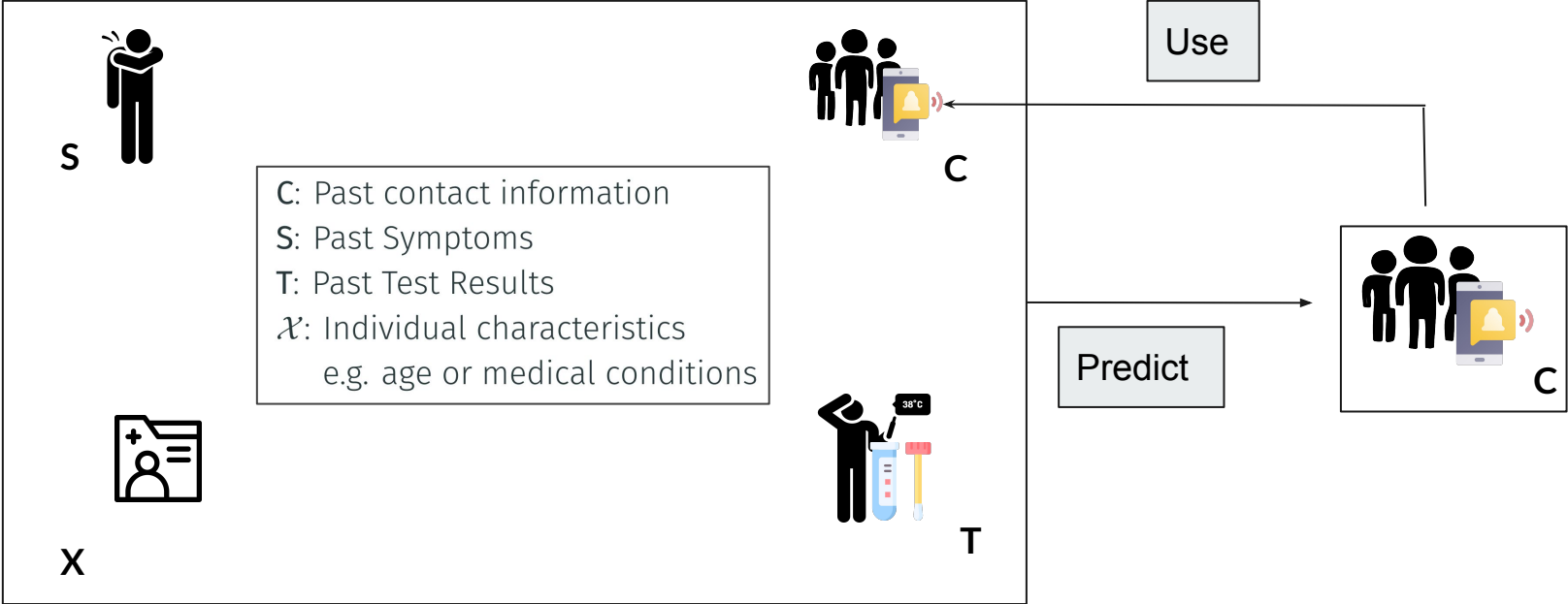
Send **secure messages** to previous contacts



**Recommend user behavior** based on **assessed risk levels**  
E.g. normal (green), wear mask/self-isolate (blue), quarantine (red)



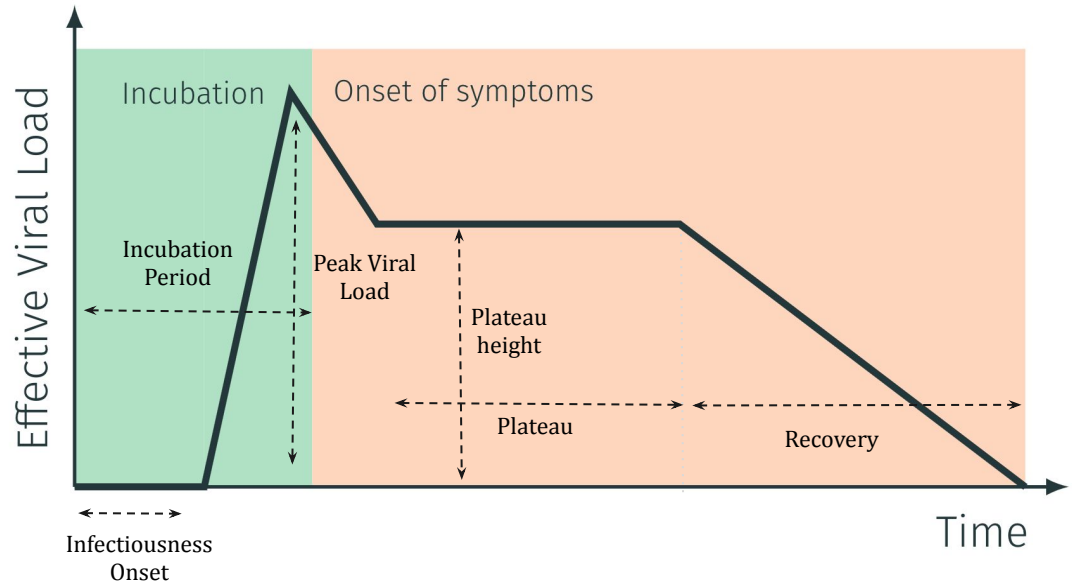
# Clues used by PRA



# Viral Load Curve

$\chi$  Individual Characteristics

$\nu(t)$  Functional form of Effective Viral Load (Contagiousness)



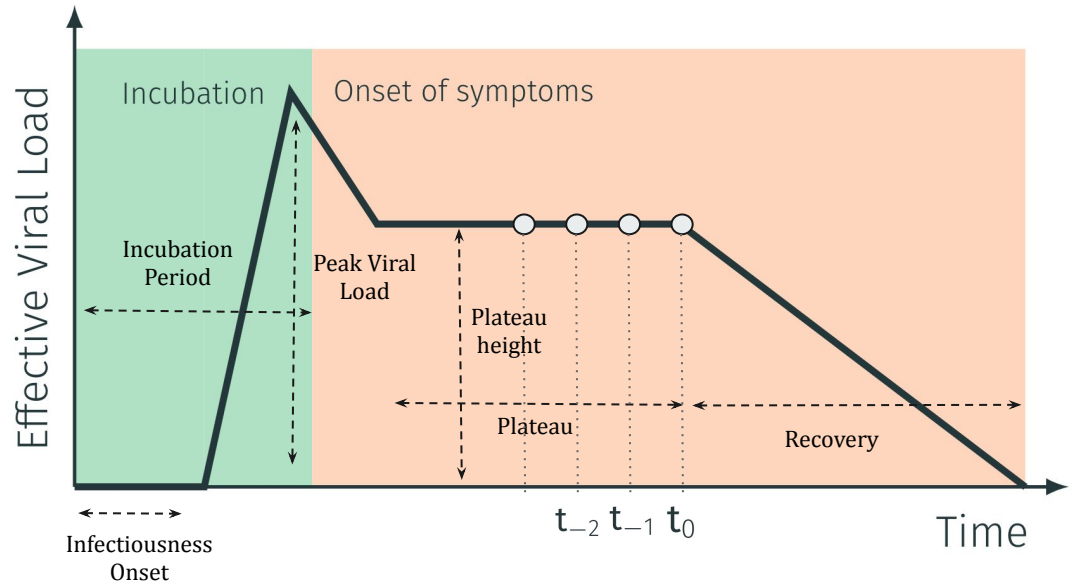
# Viral Load Curve

$\chi$  Individual Characteristics

$\nu(t)$  Functional form of Effective Viral Load (Contagiousness)

For simplicity, we consider Effective Viral Load for each day in the past 14 days -

$\nu(t_{-14}, t_{-13}, \dots, t_0)$



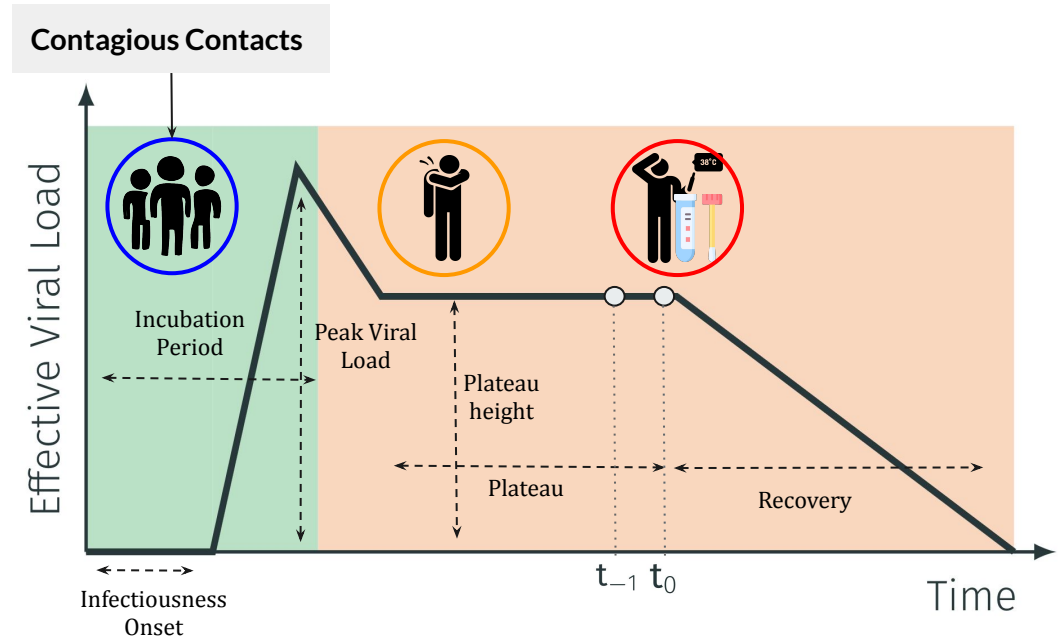
# How simulated Viral Load Curve produces observables

$$\mathcal{V}(t) = f(\text{Contacts}, \mathcal{X})$$

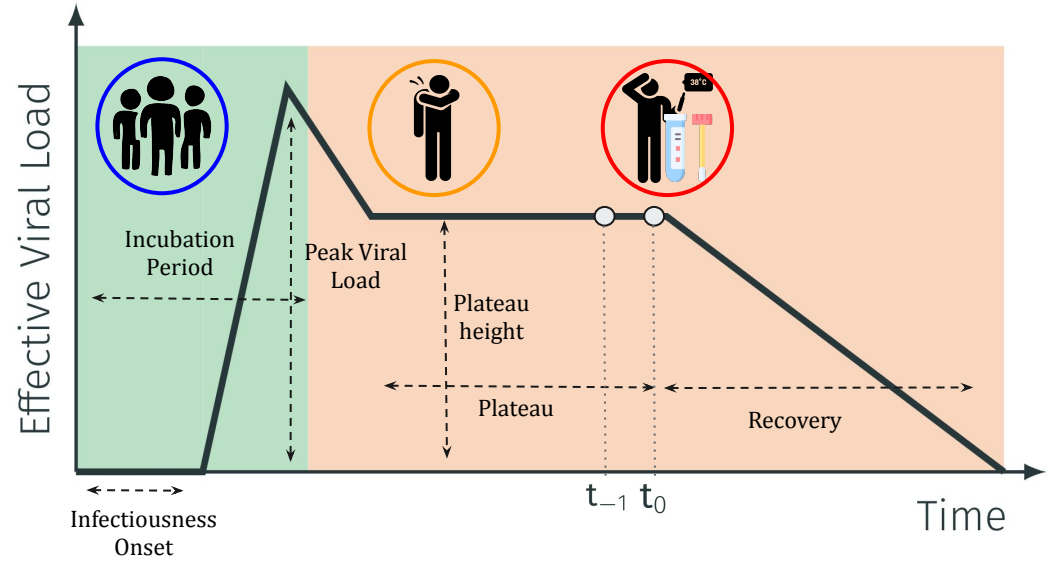
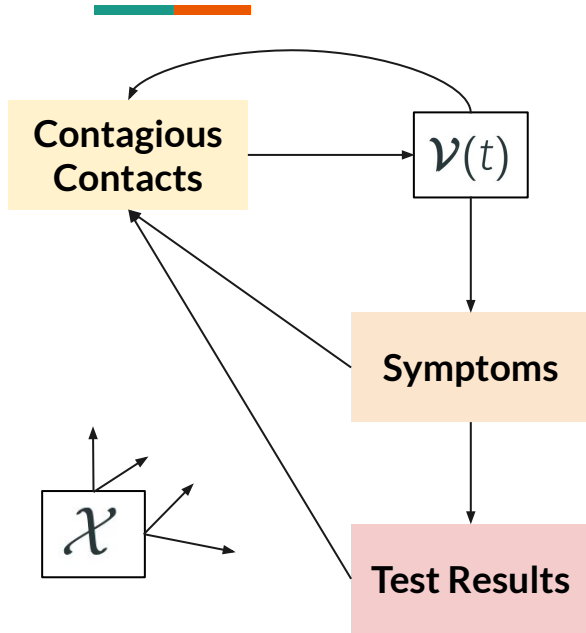
$$\text{Symptoms}(t) = f(\mathcal{V}(t), \mathcal{X})$$

$$\text{TestResults} = f(\mathcal{V}, \text{Symptoms}, \mathcal{X})$$

$$\text{Contacts} = f(\mathcal{V}, \text{Symptoms}, \text{TestResults}, \mathcal{X})$$



# Vicious Circle



# What to predict?

$$\mathcal{V}(t) = f(\text{Contacts}, \mathcal{X})$$

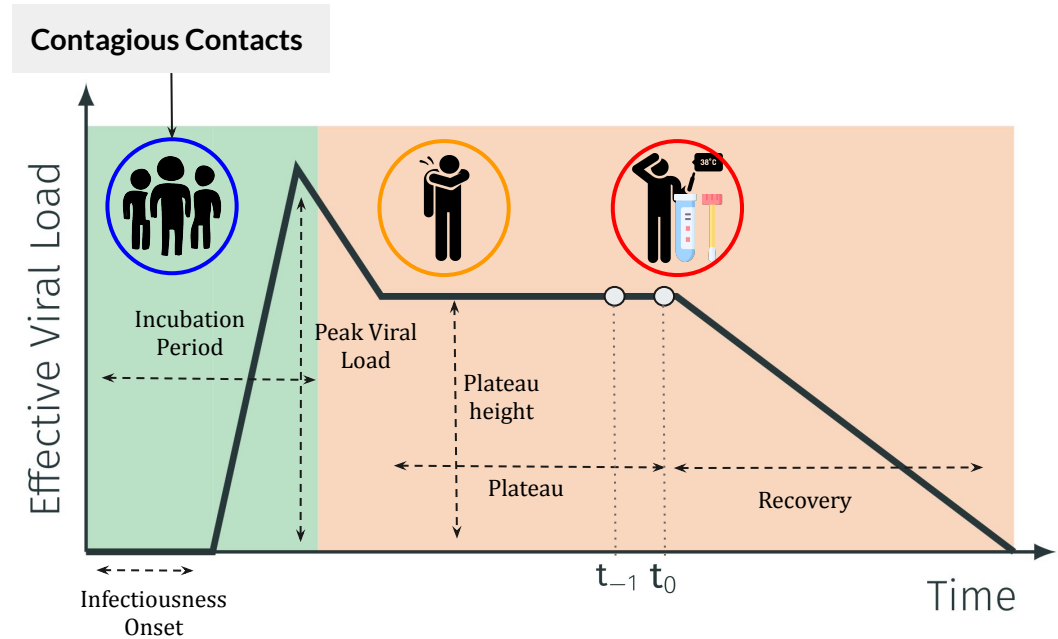
$$\text{Symptoms}(t) = f(\mathcal{V}(t), \mathcal{X})$$

$$\text{TestResults} = f(\mathcal{V}, \text{Symptoms}, \mathcal{X})$$

$$\text{Contacts} = f(\mathcal{V}, \text{Symptoms}, \text{TestResults}, \mathcal{X})$$

**Predict Effective Viral Load as the clues are observed**

$$\hat{\mathcal{V}}(t_{-14}, t_{-13}, \dots, t_0) = g(\mathcal{C}, \mathcal{S}, \mathcal{T}, \mathcal{X})$$



# PRA: Predict - Inform - Advice

C: Past contact information

S: Past Symptoms

T: Past Test Results

$\mathcal{X}$ : Individual characteristics  
e.g. age or medical conditions



Predict **today's and past contagiousness** using all the clues i.e.

$$\hat{v}(t_{-14}, t_{-13}, \dots, t_0) = g(C, S, T, \mathcal{X})$$



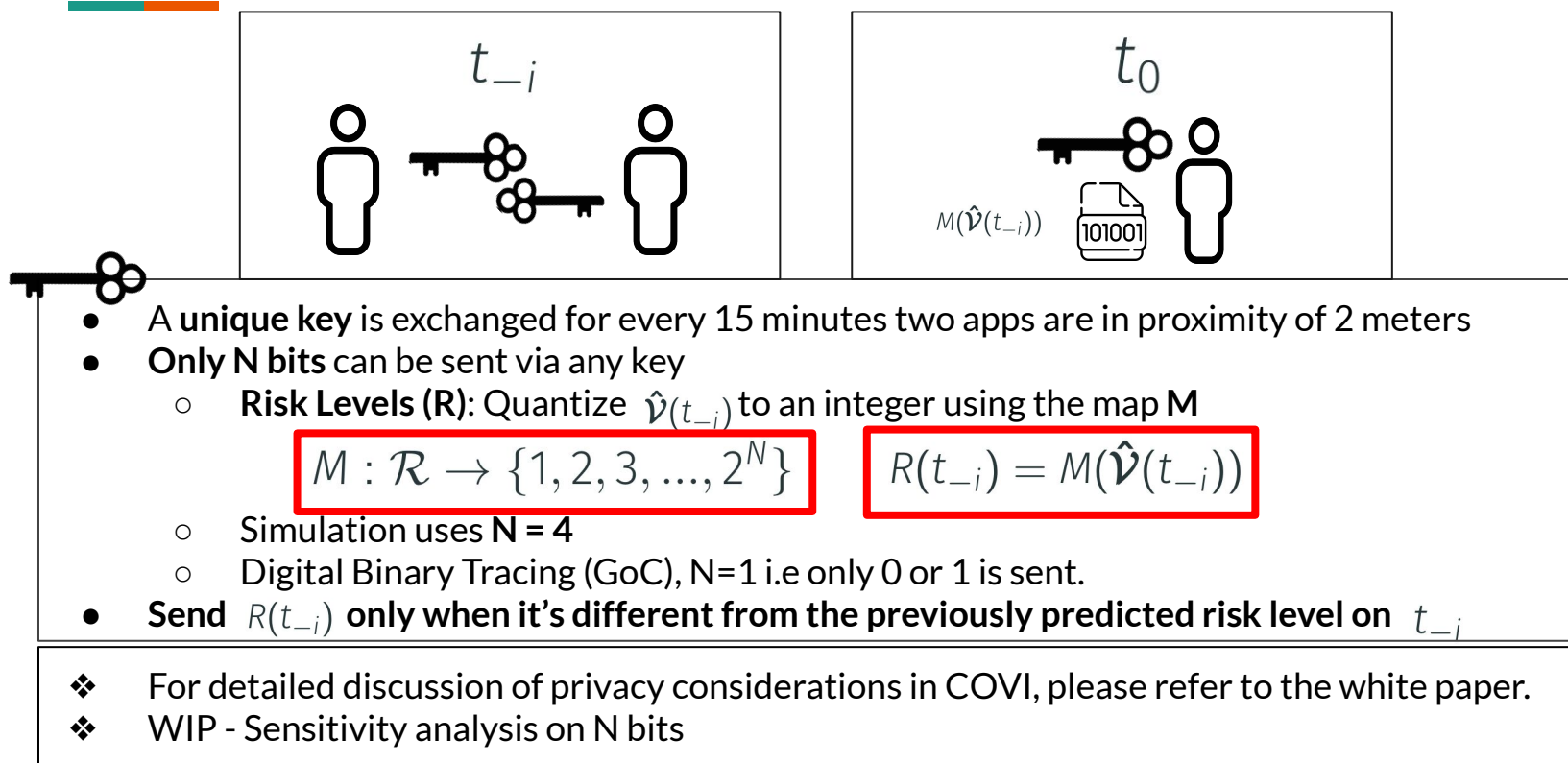
Send  $\hat{v}(t_{-i})$  to the contacts on day  $t_{-i}$

Add it to C of the **contact** and repeat



Use  $\hat{v}$  to **recommend user behavior**  
e.g. quarantine, wear mask, self-isolate, etc.

# Privacy Preserving PRA





# PRA: Predict - Inform - Advice

C: Past contact information  
S: Past Symptoms  
T: Past Test Results  
 $\mathcal{X}$ : Individual characteristics  
e.g. age or medical conditions



Predict **today's and past contagiousness** using all the clues i.e.

$$\hat{v}(t_{-14}, t_{-13}, \dots, t_0) = g(C, S, T, \mathcal{X})$$





























Send  $R(t_{-i})$  to the contacts on day  $t_{-i}$

Add it to C of the **contact** and repeat



Use  $\hat{v}$  to **recommend user behavior**  
e.g. quarantine, wear mask, self-isolate, etc.

# PRA provides multi-level recommendation thanks to richer clues

	 Manual Tracing	Digital Binary Tracing 	PRA (COVI) 
Clues Used	  	 	    
Potential Contacts	 	 	 
Recommendations	 	 	  

# Heuristic PRA Supports Mobility of Individuals

## Set Risk Levels

$$R(t_{-14}, t_{-13}, \dots, t_0) = g_{Heuristic}(C, S, T)$$

**T** - If the user reports a positive test result set  $R = 15$  for the past 14 days

**T + C1.**  
Gives Digital  
Binary  
Tracing  
(GoC)

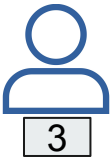
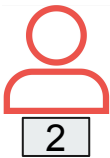
**S** - Depending on the severity of reported symptom severity, set  $R$  as

1. Severe symptoms: Set  $R=12$  for the past 7 days
2. Moderate symptoms: Set  $R = 10$  for the past 7 days
3. Mild symptoms: Set  $R = 7$  for the past 7 days

**C** - Break down all received risk levels  $R'$  into three categories

1. High ( $R' \geq 12$ ): Set  $R = R' - 5$  until the day of receipt of  $R'$
2. Medium ( $10 \leq R' < 12$ ): Set  $R = R' - 5$  until the day of receipt of  $R'$
3. Mild ( $R' < 10$ ): Set  $R = R' - 5$  until the day of receipt of  $R'$

## User Recommendations

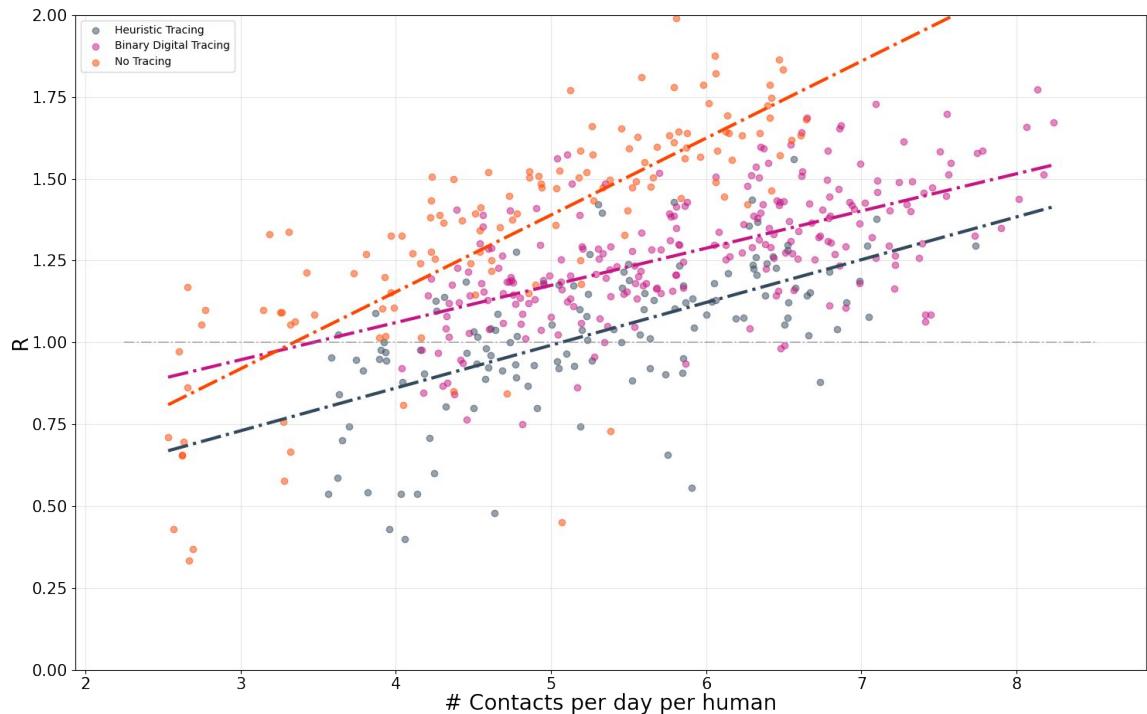


Finally, take the max of risk levels on each day obtained from above computation

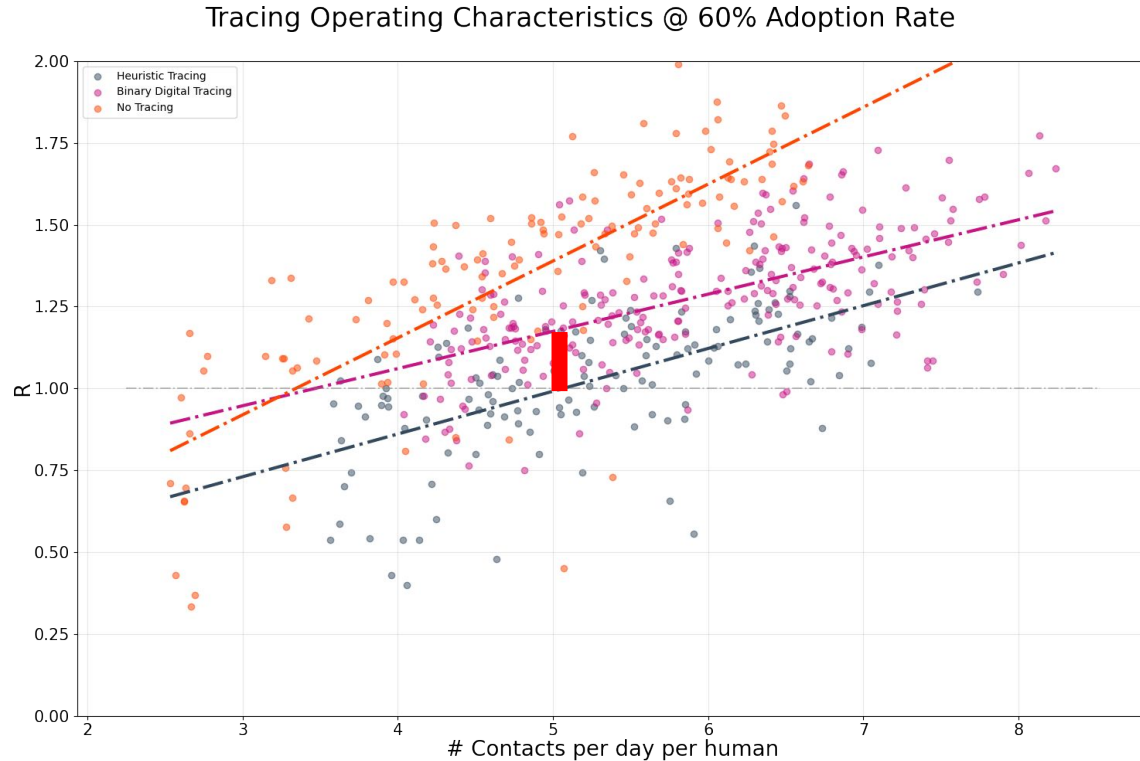
# Simulation Results: COVI Balances Mobility and Virus Transmission (R)



Tracing Operating Characteristics @ 60% Adoption Rate



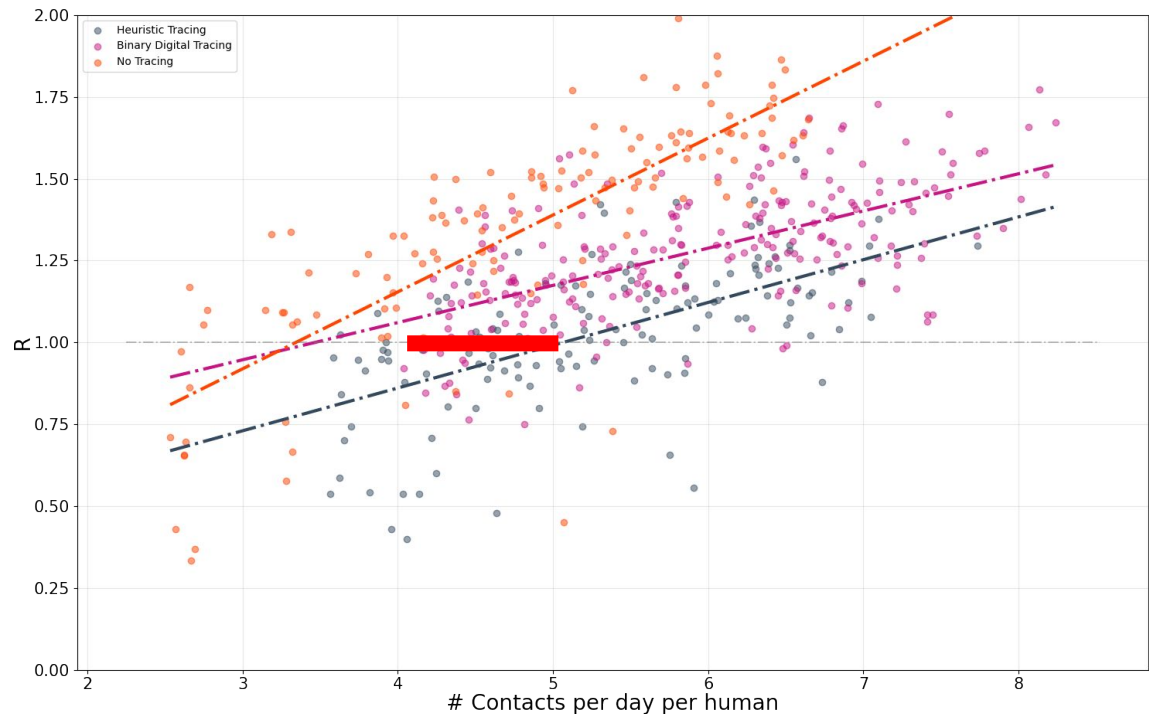
# Simulation Results: COVI Balances Mobility and Virus Transmission (R)



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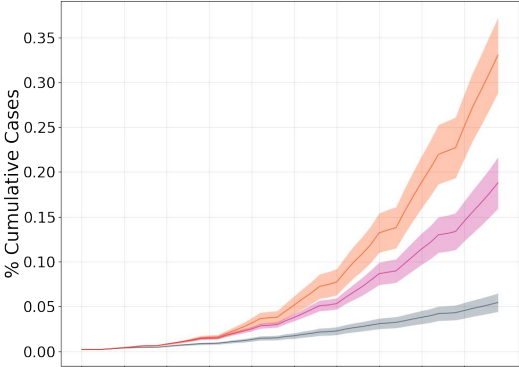


Tracing Operating Characteristics @ 60% Adoption Rate

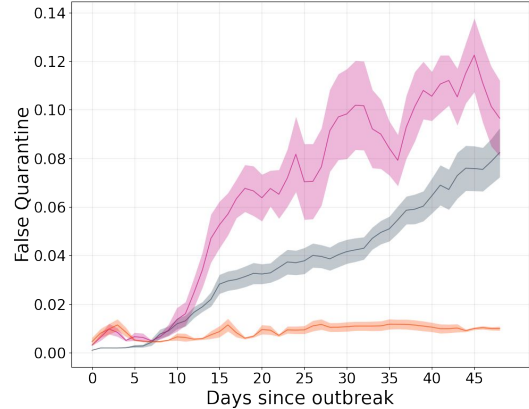
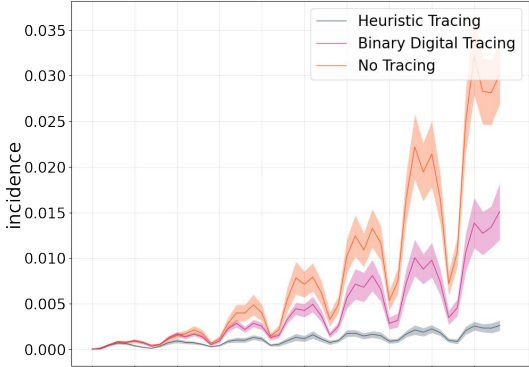
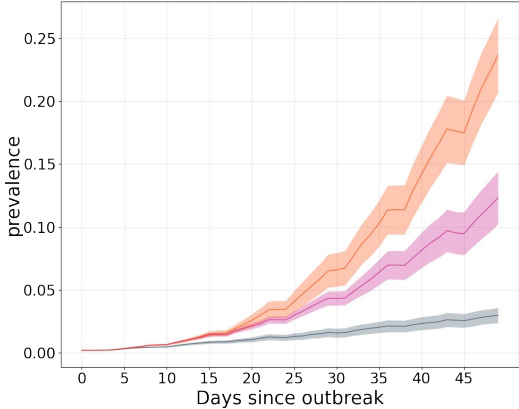


# Simulation Results: Improved Case Curves Under COVI

Fraction of infected population up to date



Fraction of population infected at any point in time



Average risk of infection

Average % population not infected but quarantined

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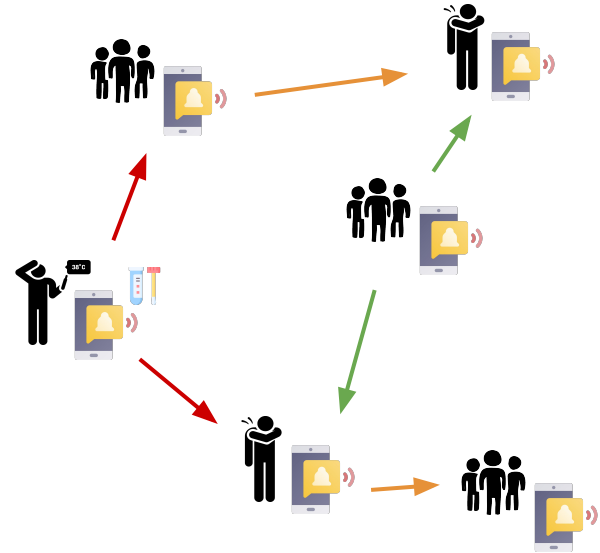
# Why Machine Learning?



# Why Machine / Deep Learning?



- It's tricky to decide what messages one user should send to the other about its risk.
  - In Binary Digital Tracing (BDT, GoC App), the decision is based on the test results.
  - But can we do better at sending early warning signals?
- Machine learning enables us to **learn** to decide what messages to send using real and simulation data in an automated and scalable way.

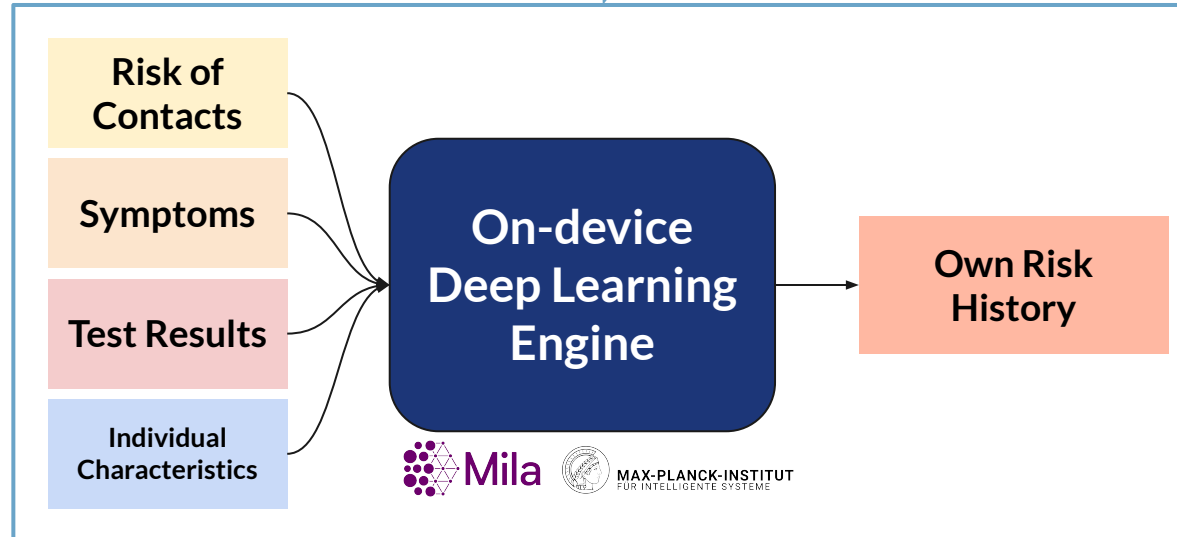
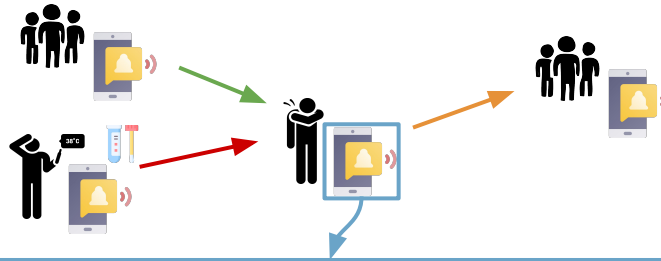


# Example Scenario: Better Early Warning Signals

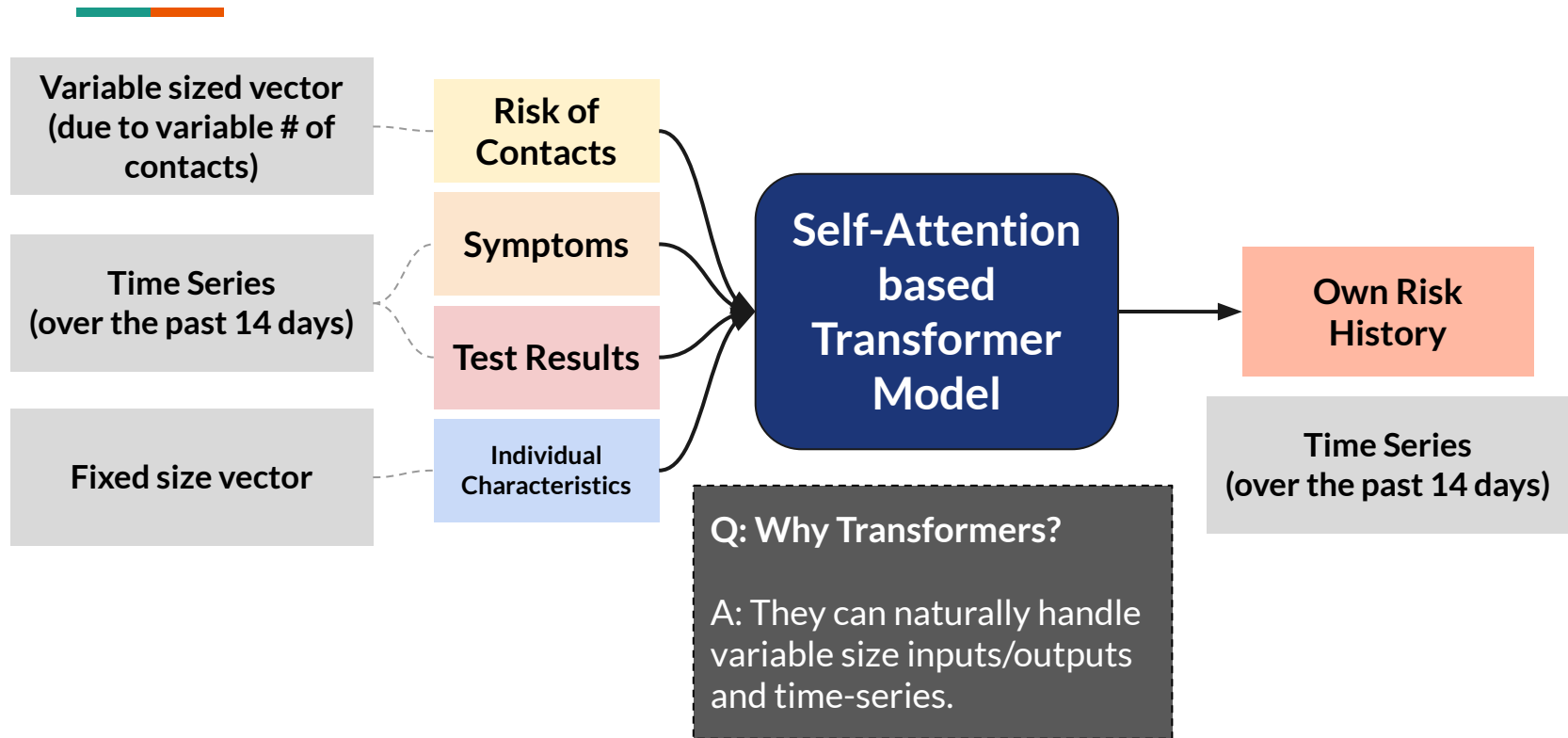


	M	T	W	T	F	S	S	M	T	W	T	F	S	S
<b>Manual tracing only</b>			Jim has a contact with high-risk stranger at the grocery store		Stranger starts showing symptoms		Stranger's symptoms grow worse	Jim GOES to work	Stranger sees doctor, gets tested	Test result comes back positive			Jim is contacted directly by public health	
<b>Binary contact tracing</b>	Jim installs the app		Jim has a contact with high-risk stranger at the grocery store		Stranger starts showing symptoms		Stranger's symptoms grow worse	Jim GOES to work	Stranger sees doctor, gets tested	Test result comes back positive			Jim is contacted directly by public health	
<b>Our approach</b>	Jim installs the app		Jim has a contact with high-risk stranger at the grocery store		Stranger starts showing symptoms		Stranger's symptoms grow worse	Jim DOES NOT go to work	Stranger sees doctor, gets tested	Test result comes back positive			Jim is contacted directly by public health	

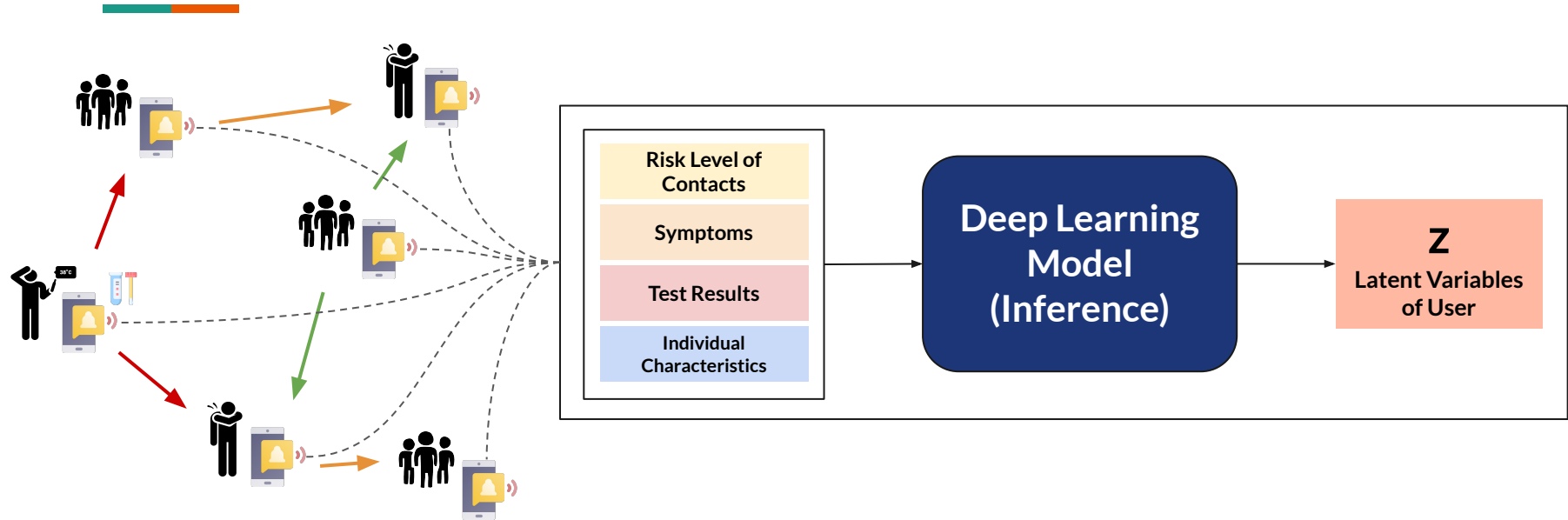
# What happens on the phone?



# The Deep Learning Engine Unboxed

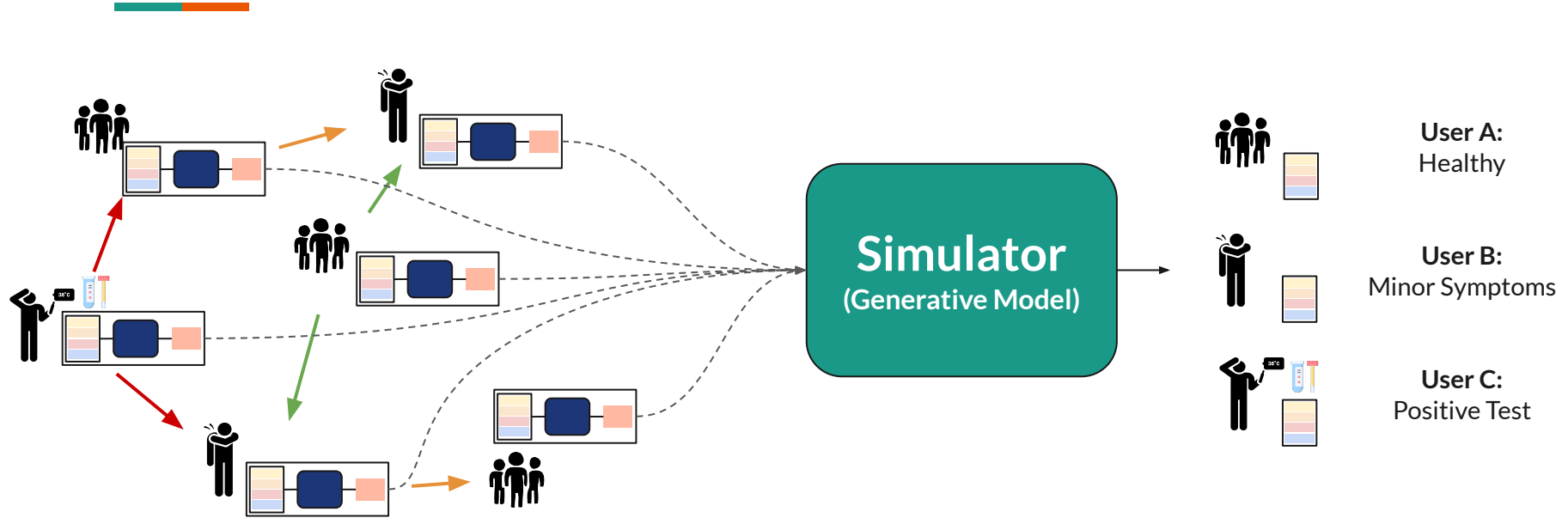


# Learning from Real World Data (Work in Progress!)



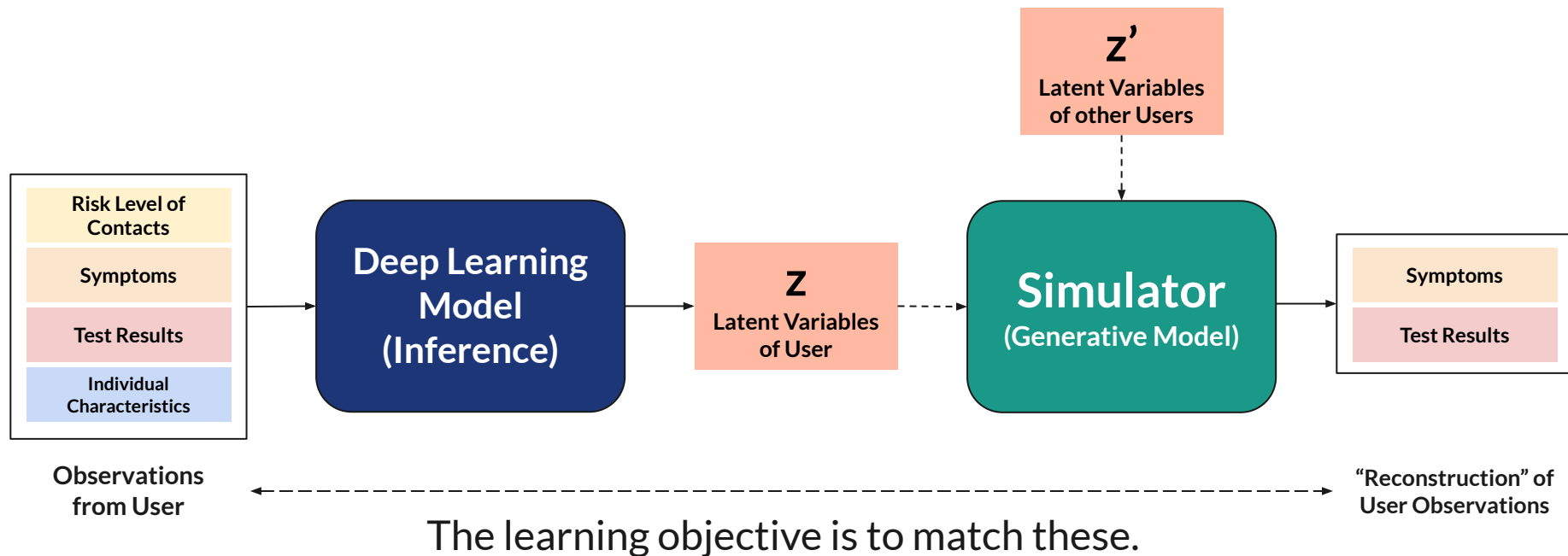
The “inference model” runs on every app-users’ phone.

# Learning from Real World Data (Work in Progress!)

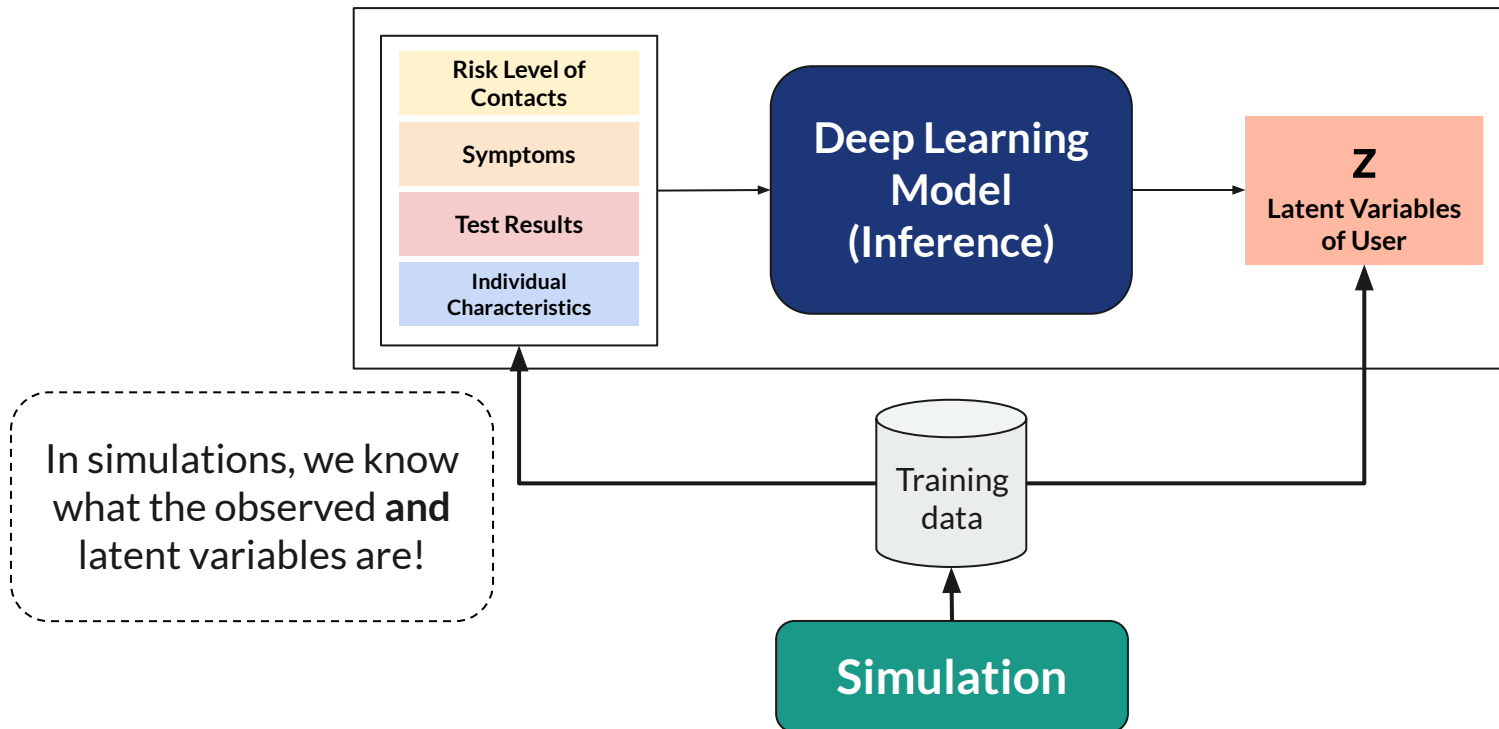


The “generative model” receives latent variables from every app user (who has consented), and predicts their respective states.

# Learning from Real World Data (Work in Progress!)

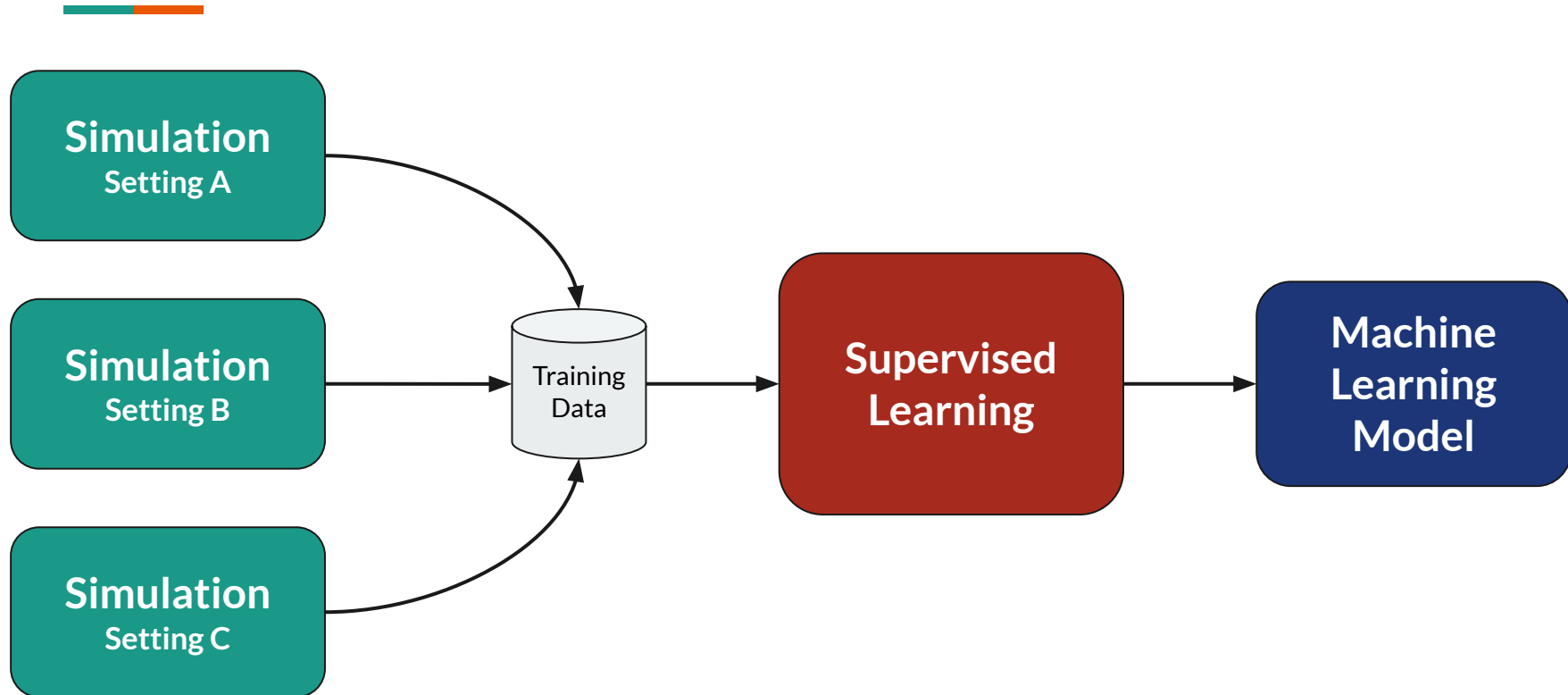


# Milestone: Learning from Simulations

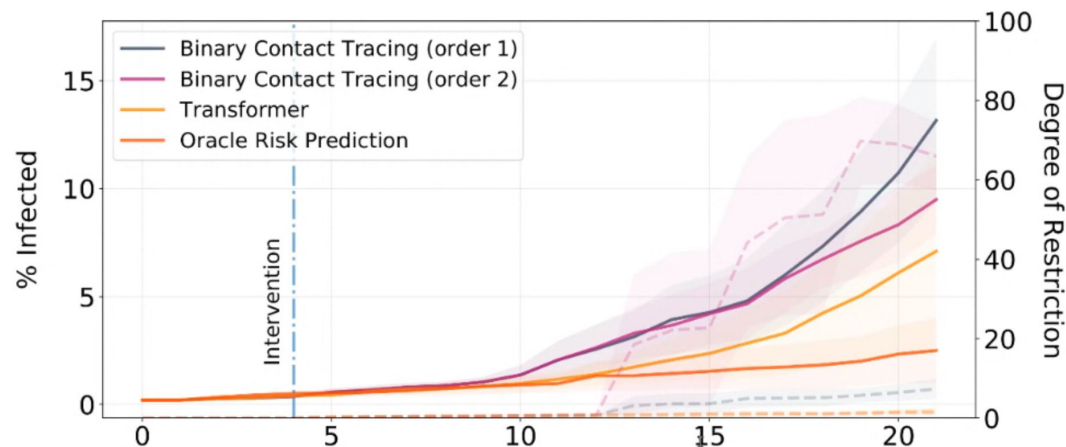




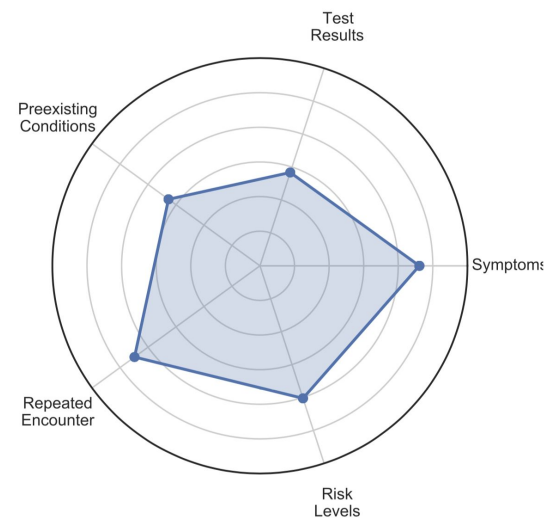
# Learning from *Domain Randomized* Data



# First Results



The transformer controls the infection better than BDT  
(while being less constraining)

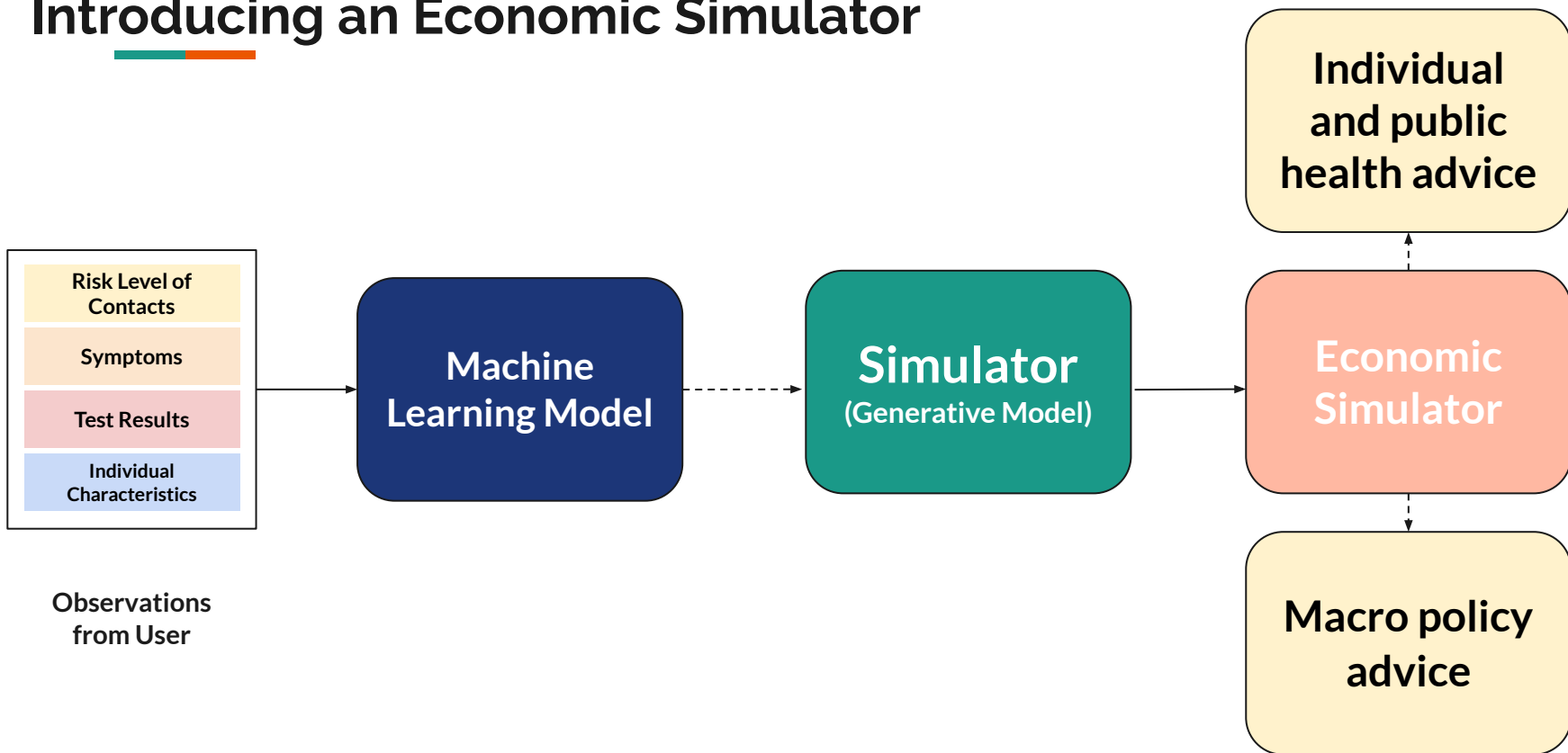


Importance of input features  
for the transformer

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# The Health and Economic Impacts of Tracing

# Introducing an Economic Simulator

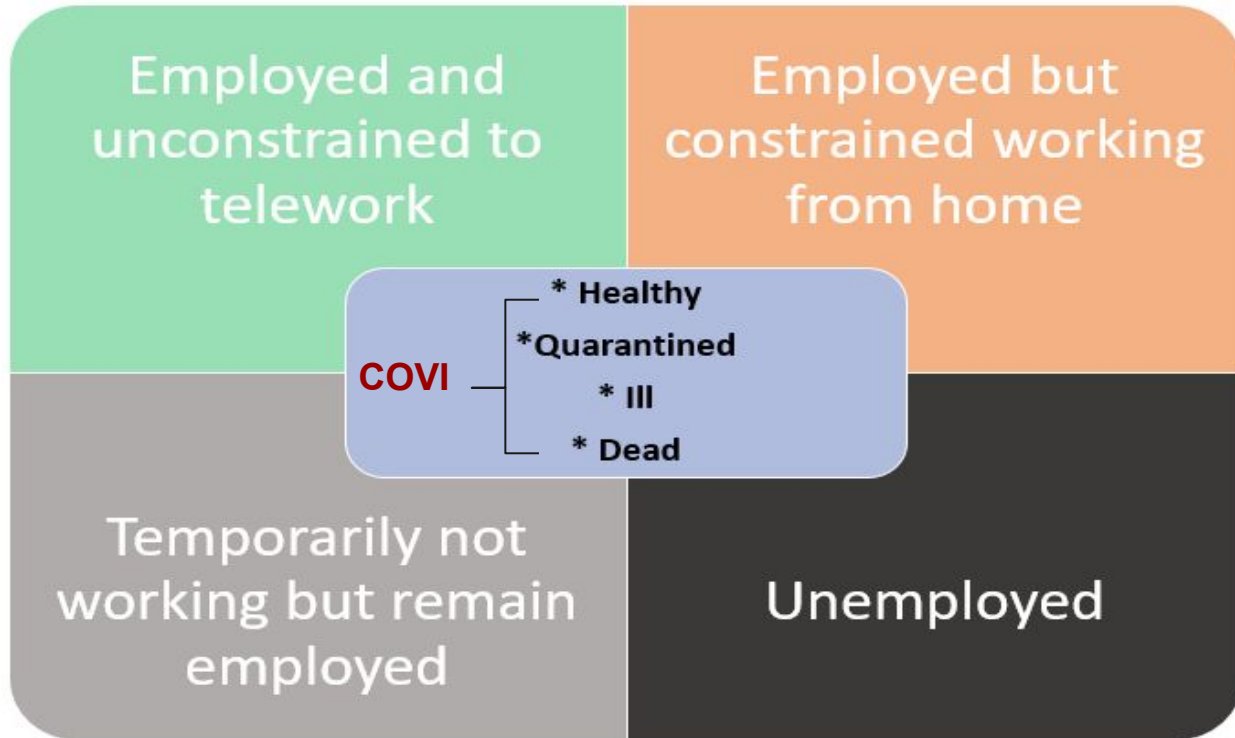


# adaptER-COVID19: an application to national data

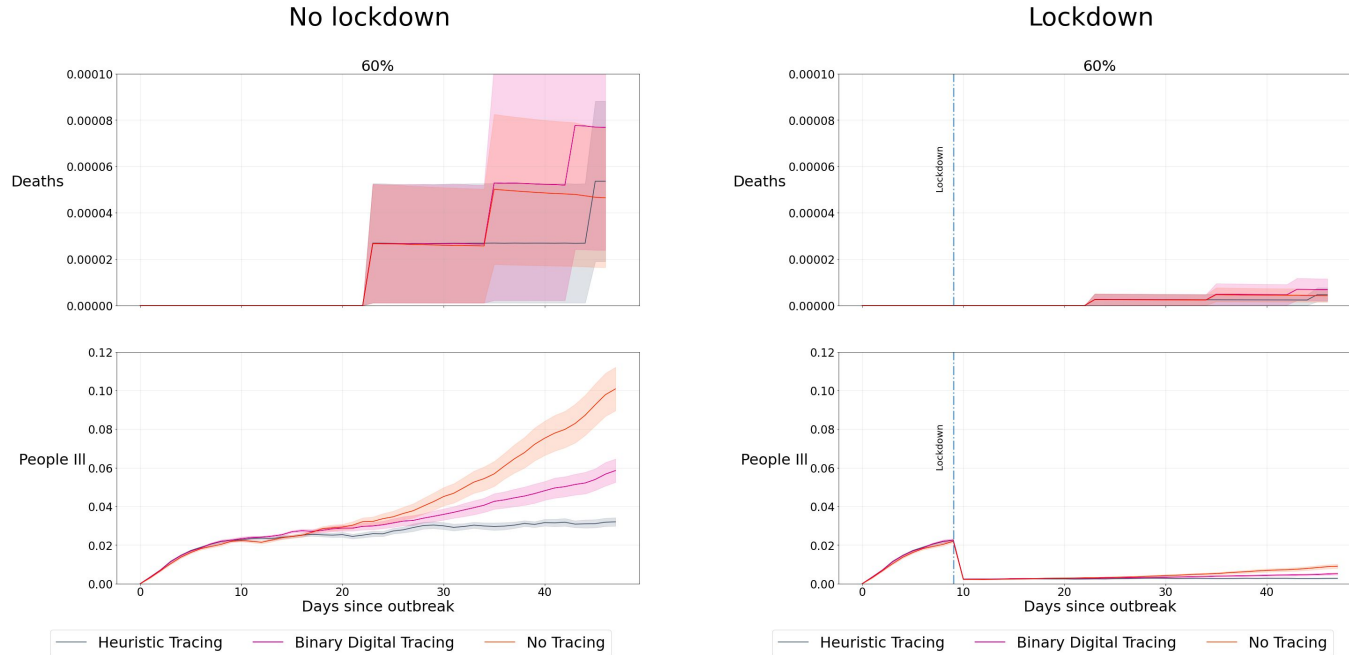
01	Input-output Model	<ul style="list-style-type: none"><li>• Labour, capital, imports as inputs for production</li><li>• Consumption, investment and export sectors</li></ul>
02	Corporate Bankruptcy Model	<ul style="list-style-type: none"><li>• Agent-based corporate defaults</li><li>• Connected to IO-Model through net operating surplus of companies</li></ul>
03	Individual Insolvency Model	<ul style="list-style-type: none"><li>• Model household earnings</li><li>• Behavior (fear factor) determining risk of insolvency</li></ul>

Source: <https://github.com/BDI-pathogens/OpenABM-Covid19>  
<https://www.coronavirus-fraser-group.org/>

# Mapping COVI into a matrix of employment & health status

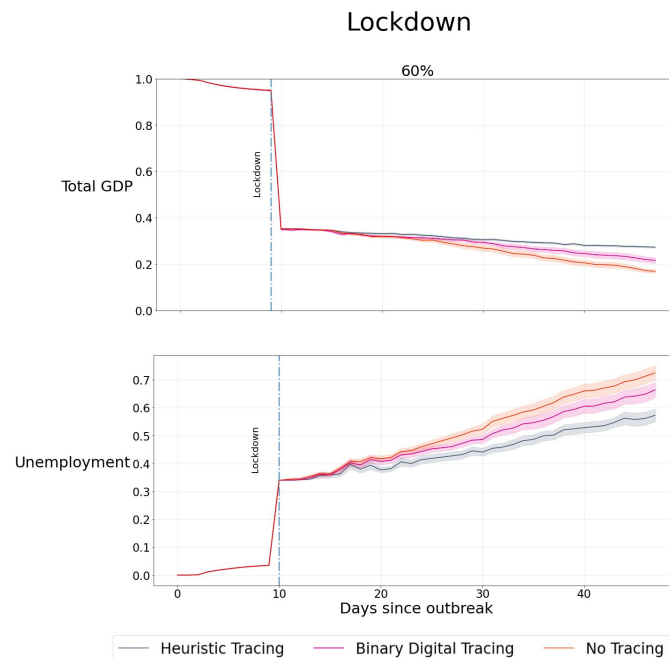
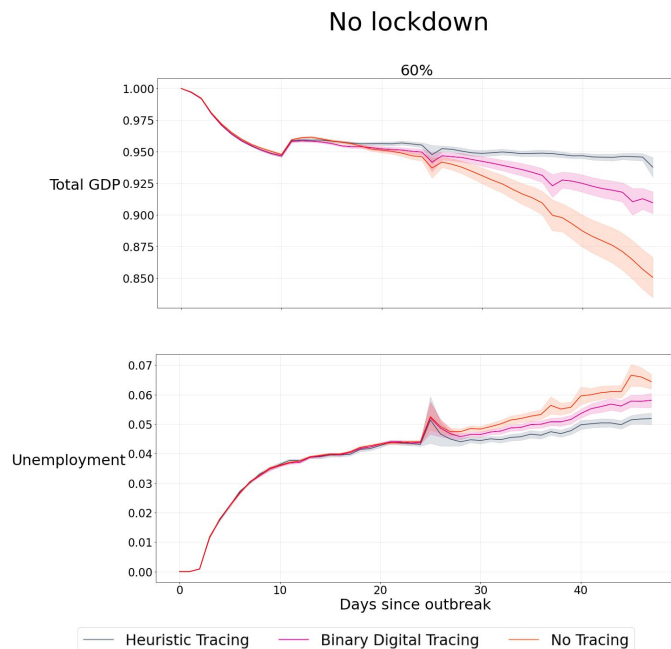


# COVI improves health outcome (lower # of ill and deaths)...



Source: “The Daily - Study: Willingness of Canadians to use a contact tracing application”, Statistics Canada. July 31, 2020.  
<https://www150.statcan.gc.ca/n1/daily-quotidien/200731/dq200731d-eng.htm>

... while incurring smaller economic cost (higher GDP & lower U rate)









# Some limitations in adapterER - COVID19



- **I-O model uses accounting identity, no pricing optimization**
  - Switching to realistic production function considering input substitutability
- **Modelling labour and capital market may benefit from general equilibrium models**
  - Workers don't have the ability to switch jobs
  - No part-time, self-employment
- **Don't account for interest payments and leverage of firms**

## ACTION: Expand the Health-Economic Frontier with Technology!

	 <b>No Tracing</b>	<b>Digital Binary Tracing</b> 	<b>PRA (COVI)</b> 
<b>Individual mobility (social wellbeing)</b>	High, but at risk of forced lockdown	Low	Intermediate
<b>Infection Transmission rate (R0)</b>	High	Intermediate	Low
<b>Economic impact (GDP, jobs)</b>	Poor	Intermediate	 <b>Improved</b>



# Appendix

# Future Work & Limitations & Challenges



- Scalability of simulations
- Sensitivity Analysis on privacy parameters / economical scenarios / (WIP)
- Pilot cohort study
- Deployment in developing countries
- Evaluation of risk of getting infected
- Running AdaptER-Covid19 on Canadian Datasets with support mechanisms

# Ethical considerations



- Ensured privacy based on decentralized approach to data
- Cryptographic technology for risk information notification
- Pseudonymized nature of optional volunteered data
- Governance and inclusivity

# Preliminary Simulations



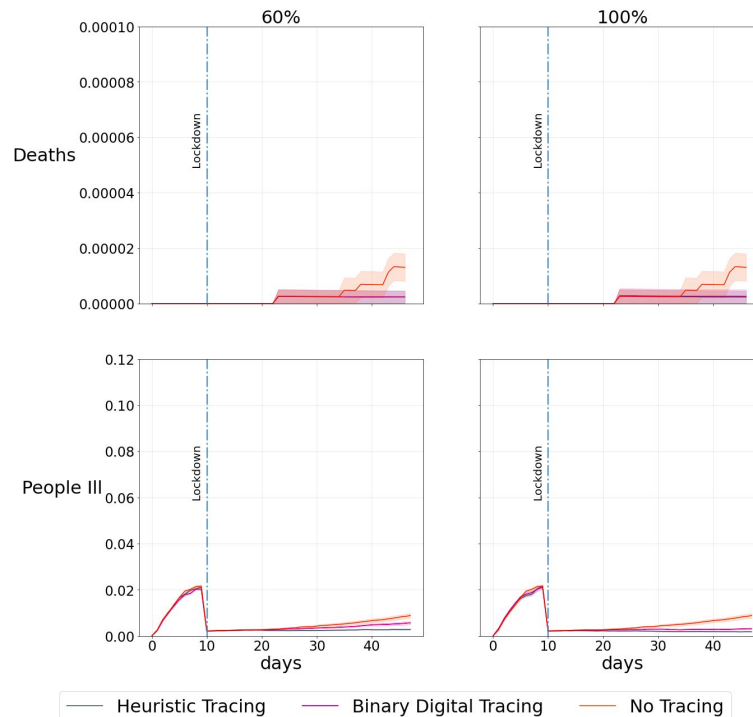
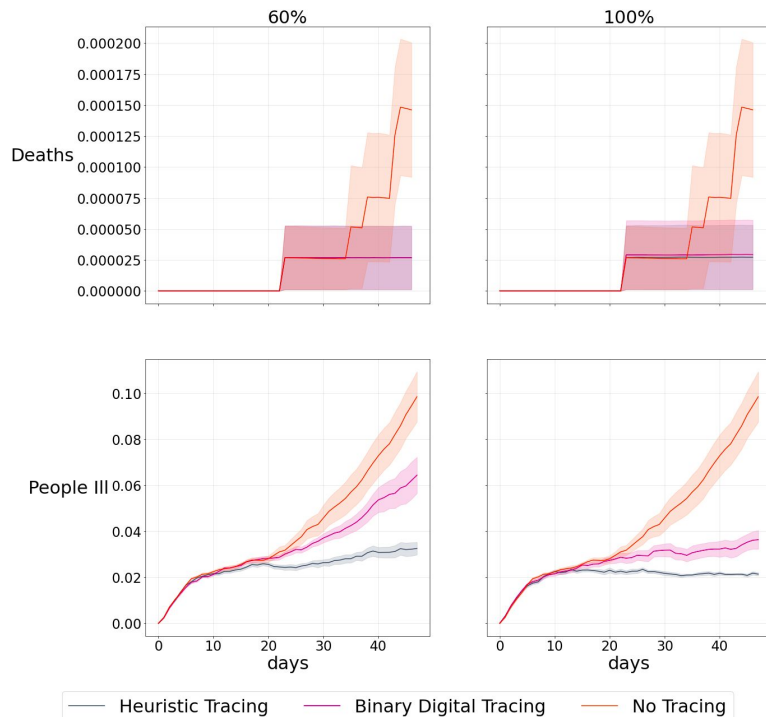
- Population size: 3000
- Initial number of infected individuals: 6 (0.2% of the population)
- 25% Asymptomatic population
- Number of tests per day = 3 (0.1% of the population)
- Behavior Modifications -
  - Low Risk Agents have 1/8th of the contacts as compared to pre COVID-19 contacts
  - Medium Risk Agents have 1/4th of the contacts as compared to pre-COVID-19 contacts
  - High Risk Agents have 0 contacts (Quarantine)
- Adherence to recommendations is modeled via dropout of 0.02 probability of following the recommendations
- Quality of self-diagnosis is modeled via dropout on symptoms of 0.2 i.e a user is 20% likely to not report their specific symptoms

# 100% adoption rate comparison



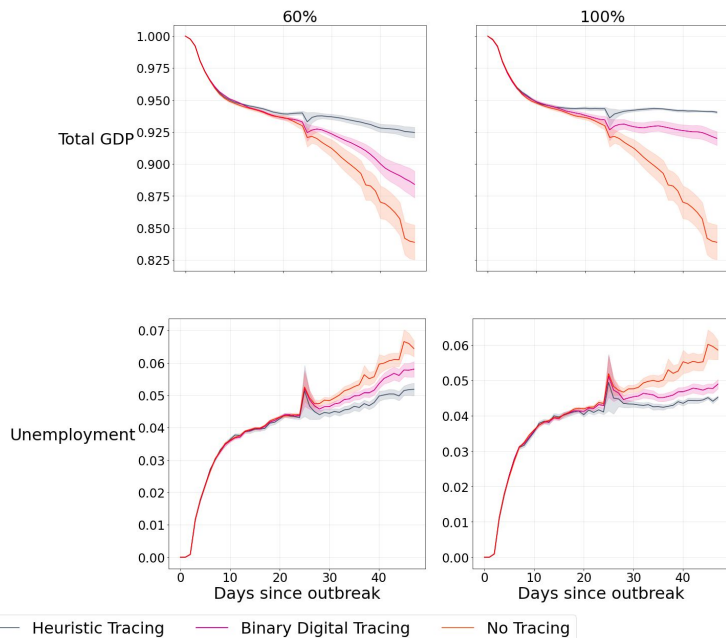
No lockdown

Lockdown



# 100% adoption rate comparison

No lockdown



Lockdown

